

High Dynamic Range, 100km

RADIO OVER FIBER LINKS



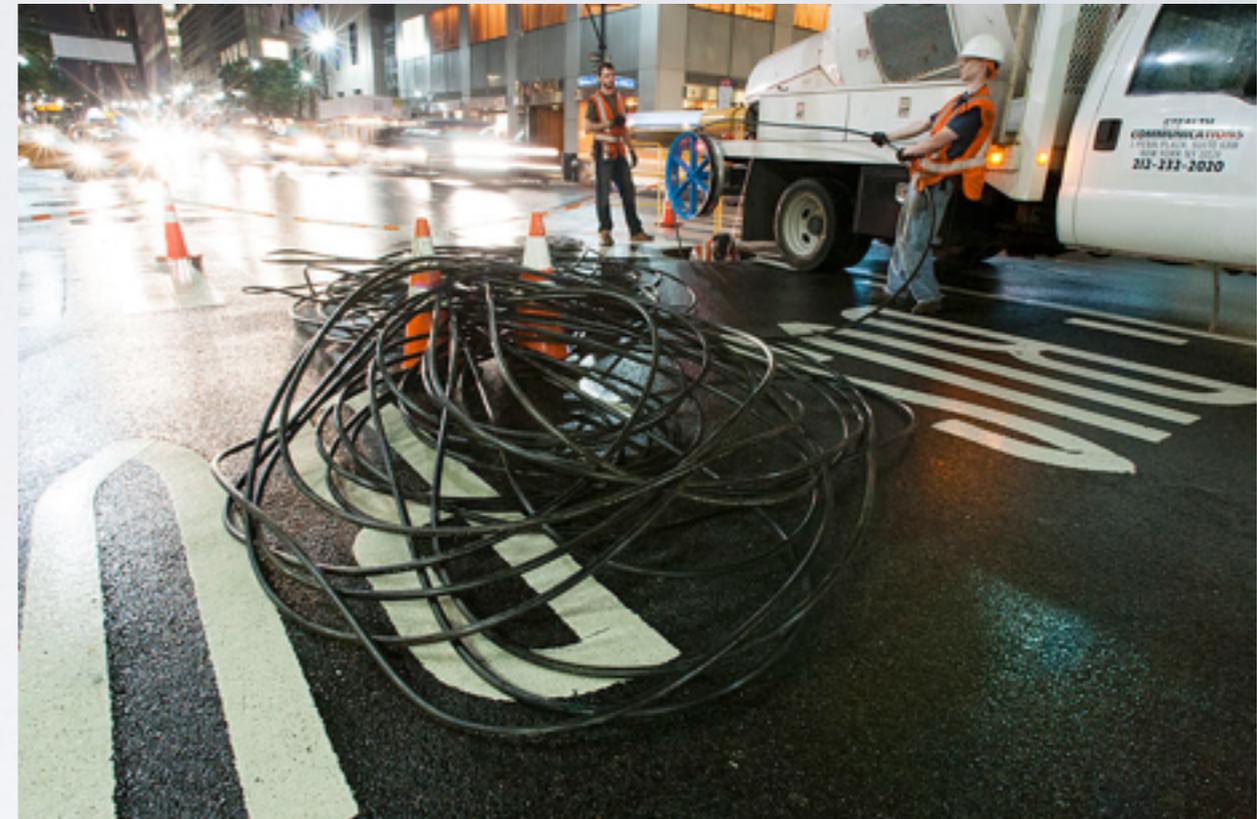
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*Data obtained in collaboration with
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US Naval Research Lab
Washington, DC*

Optical fiber is now ubiquitous

- High Capacity (Pb/s)
- Low Loss (0.2 dB/km [opt])
- Long Haul (Digital)
Transatlantic, Internet Backbone
- Last Mile (RF/ Radio Over Fiber [RoF])
FiOs, CATV, Fiber-to-the-Home



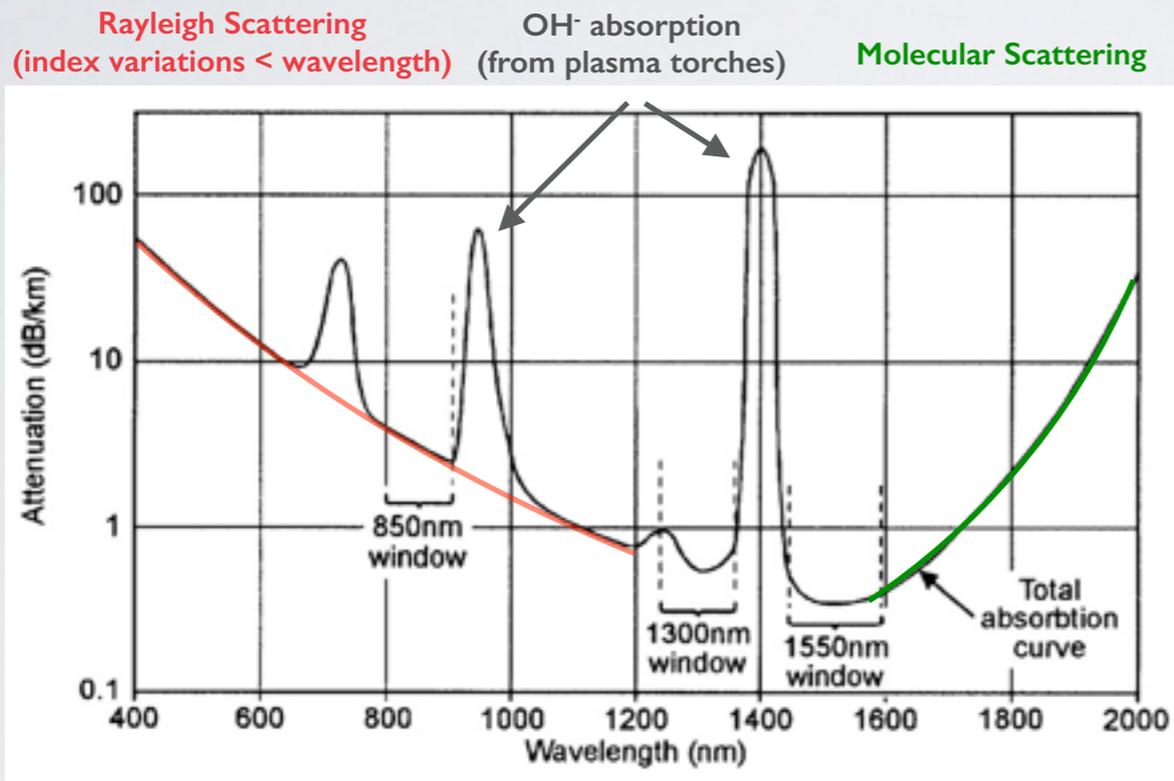
 Stealth Communications - CC3.0

Fiber delivers LOW-LOSS RF transmission over large distances

Parameter	Wireless (isotropic)	Coax (LMR-400)	Radio over Fiber
Loss@ 1km (5.8 GHz)	107 dB	354 dB	0.6 dB
Bandwidth	~10%	100%	100%
Main Issues	Regulatory Issues, Wireless Channel Impairments	Extremely High Loss	Cost/ Complexity, Dynamic Range

1550 nm is an optimal wavelength

SMF28 Fiber Attenuation



Source: nutsvolts.com

- 1550 nm - Minimum Loss Window

- 0.18 dBo/km attenuation

- Compatible with erbium doped fiber amplifiers

- Optical dispersion present

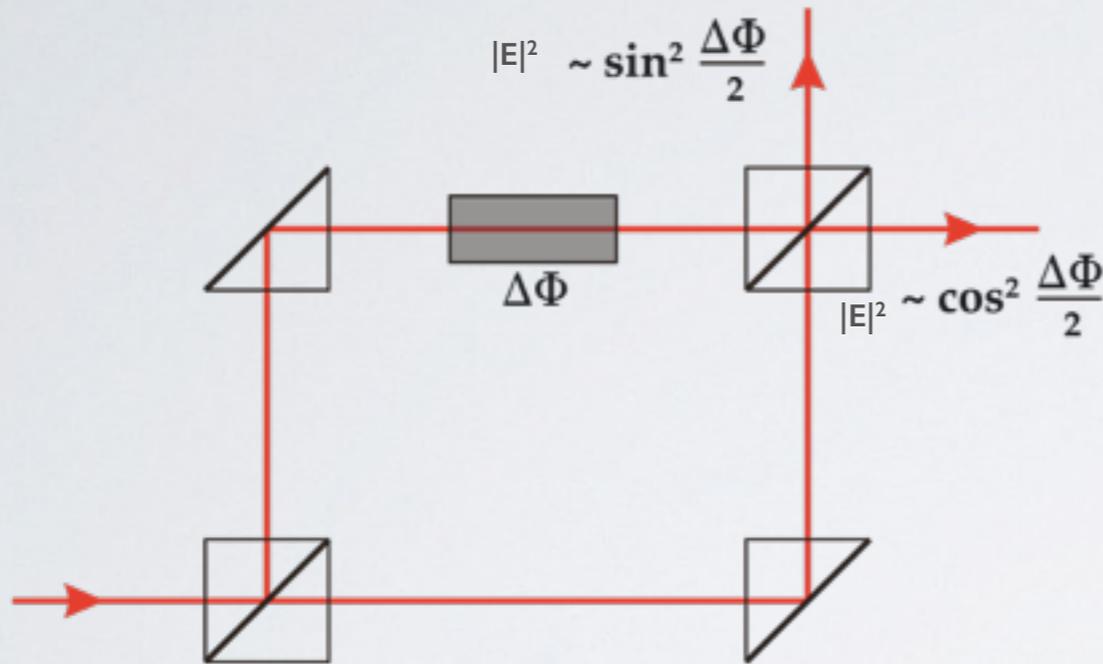
- 1310 nm - Minimum Dispersion Window

- 0.32 dBo/km attenuation

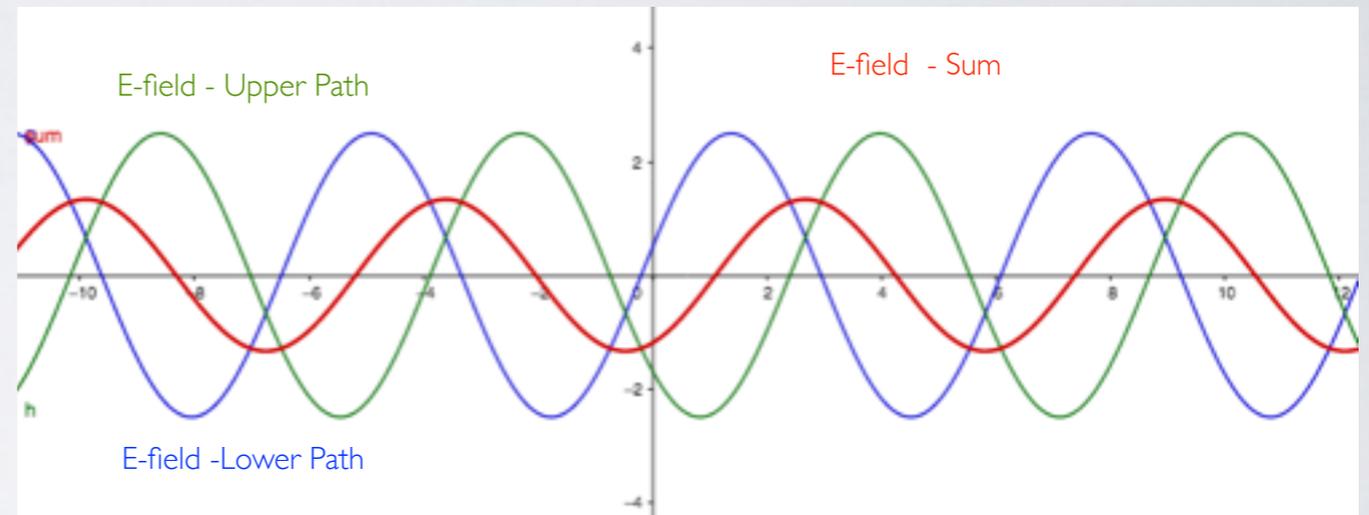
- Negligible dispersion

Note: dBo connotes optical gain/loss
dB connotes traditional RF gain/loss

PRINCIPLE: Optical interferometer



wikimedia.org

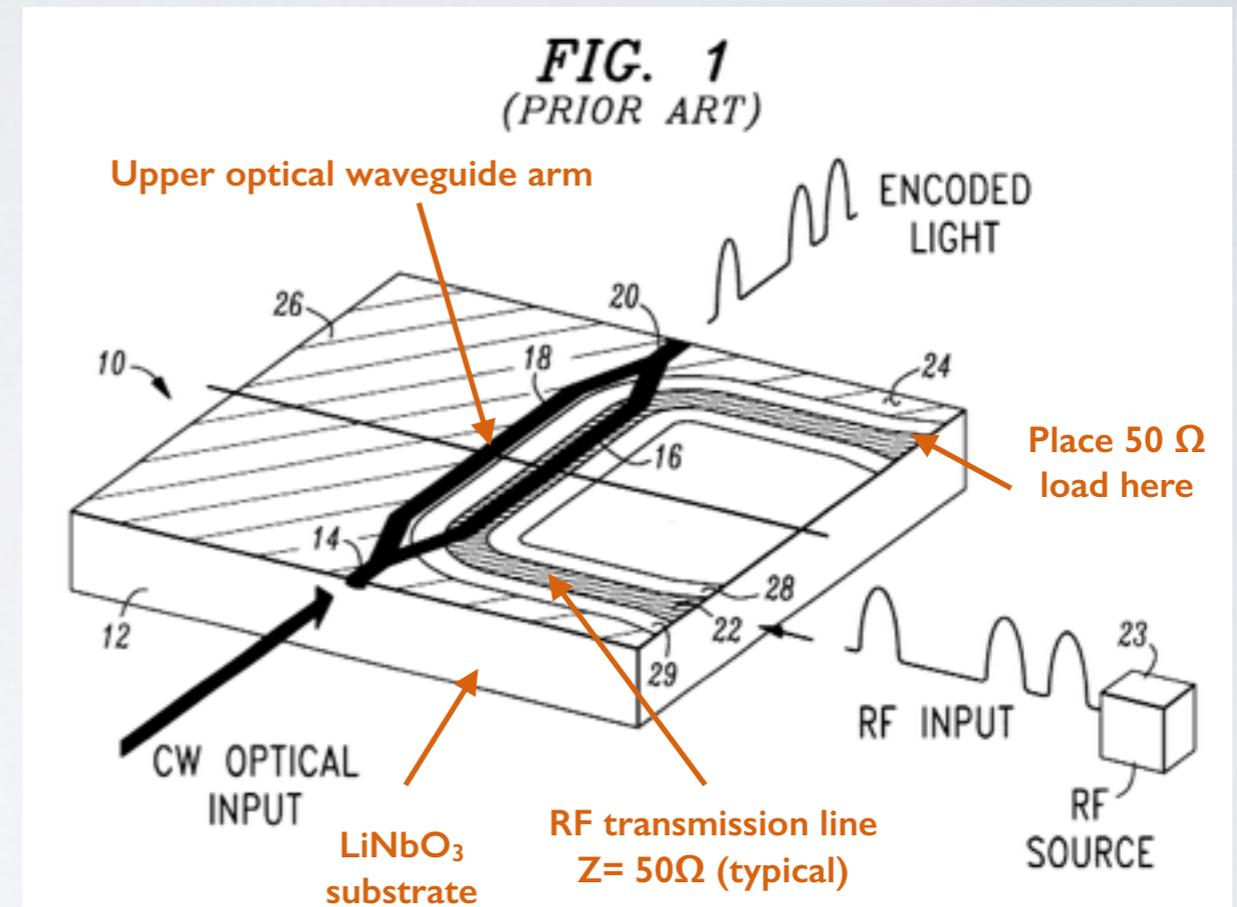


geogebra.org

- Small differences in phase ($\Delta\Phi$) between the two paths cause constructive or destructive interference.
- Interferometer converts *phase shifts* into *intensity changes*.

PRINCIPLE: The Mach Zehnder Modulator (MZM)

- The Mach Zehnder Modulator (MZM) is an **interferometer** made with optical waveguides.
- The MZM encodes changes in **input voltage** onto the **optical intensity**.
 - Step 1: Applied (RF) voltages modulate the index of refraction in the lower arm path via the electro-optic effect.
 - Step 2: Changes in index of refraction modulate the optical phase in the lower arm.
 - Step 3: When we recombine the top and bottom arms, constructive/destructive interference between the paths causes the optical intensity to change with applied voltage.
- When optical and electrical velocities are well matched, modulation bandwidth >40 GHz.

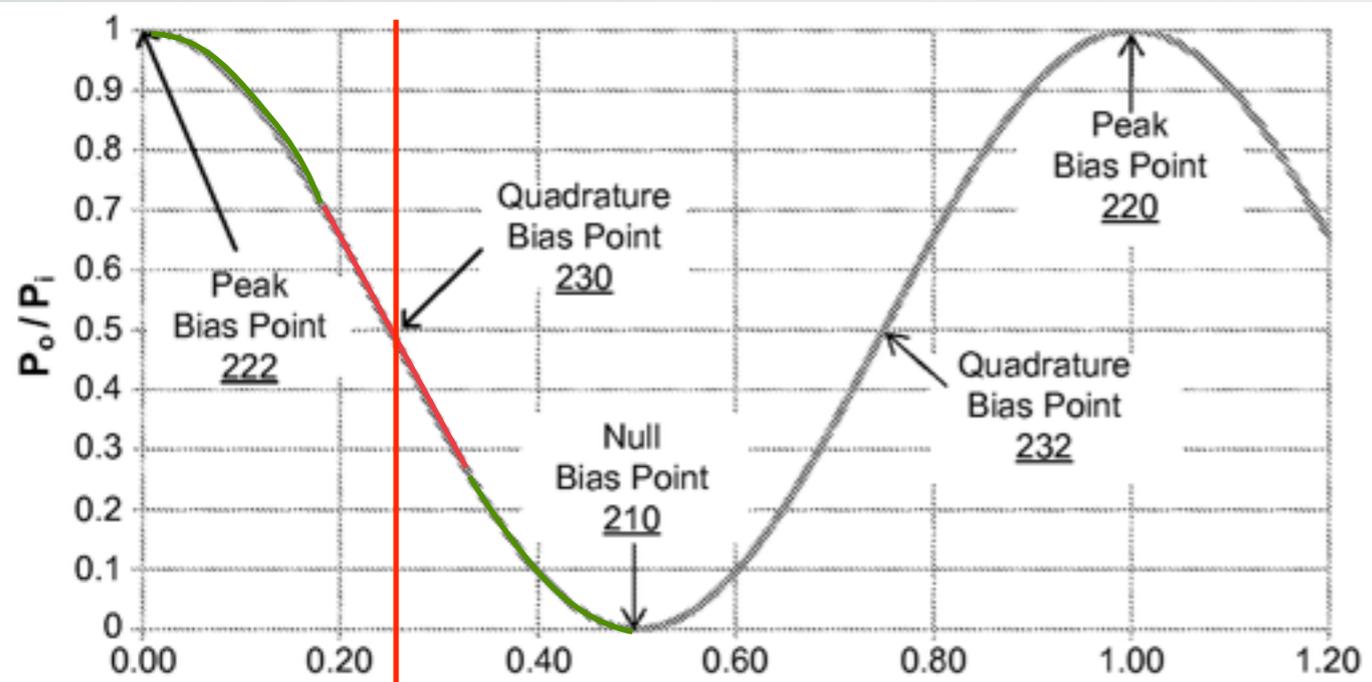


Source: Patent US6501867

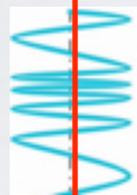
Input Optical power: P_o (1)

Input RF power (RMS): $P_{rf-in} = V_{rf-in}^2 / 2Z$ (2)

Signal Distortion depends on MZM bias setting

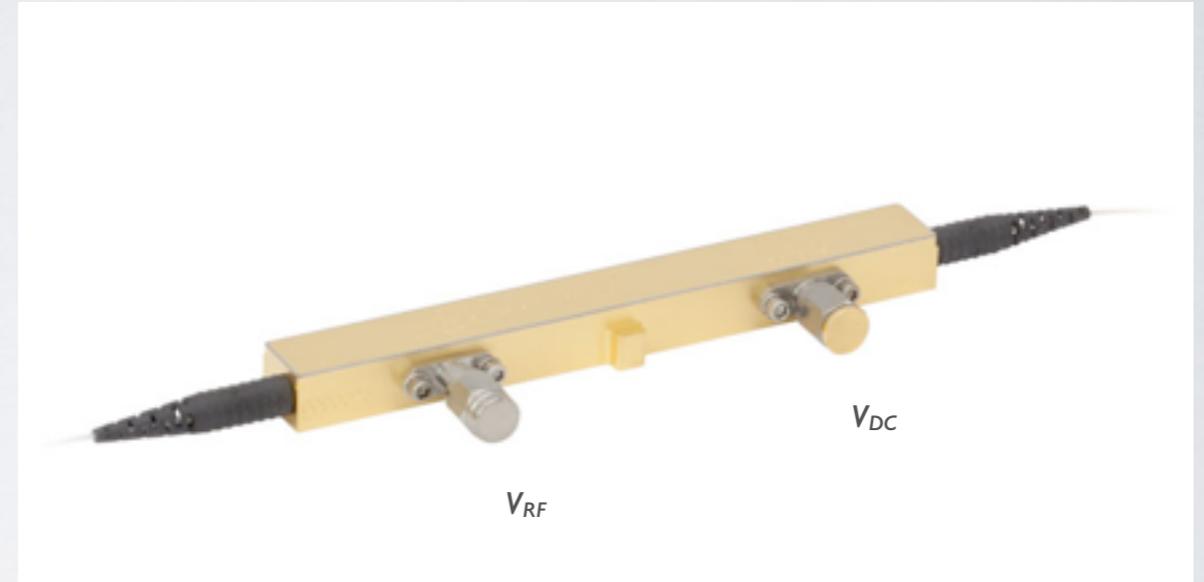


Source: Patent
US20140016172



$$V_{DC} = V_{\pi}/2$$

Electrical Input ($V/2V_{\pi}$)



ThorLabs - LN05S-FC - 40 GHz Intensity Modulator

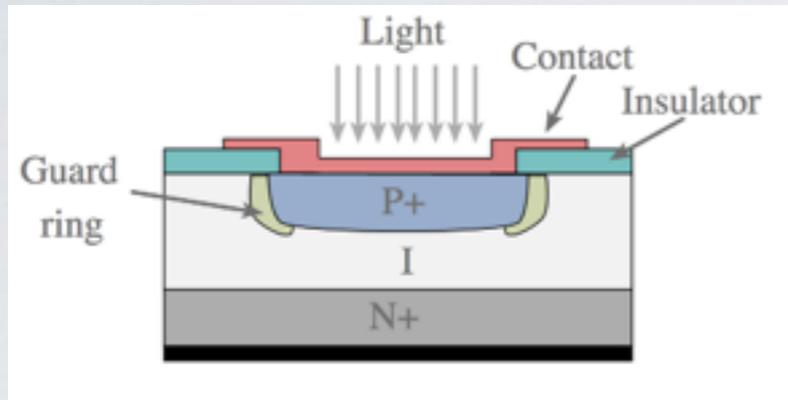
- Response is periodic in voltage, not linear
- Quadrature DC bias (50%) as shown above \Rightarrow linear portion of the response.
- Green areas excursions cause odd order distortion products
- The n th order (rms) OPTICAL INTENSITY products follow a Bessel series (just like for PM and FM in radio communications).

$$P_{mzm}(DC) = P_o/2 \quad (3)$$

$$P_{mzm}(f1) = P_o J_1(\pi V_{rf}/V_{\pi}) \quad (4)$$

etc.

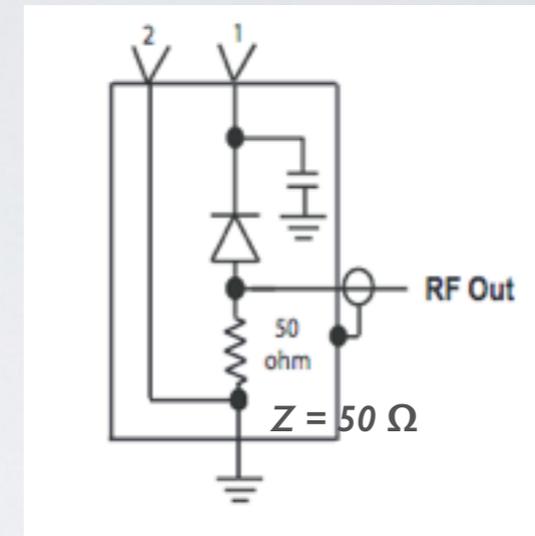
Optical-to-Electrical PIN InGaAs Photodiode



Source: electronics-notes.com



Source: Emcore -
2522 PIN Photodiode
22 GHz - 0.7 A/W@1550 nm



Source: Emcore -
2522 PIN Photodiode
22 GHz - 0.7 A/W@1550 nm

Optical Intensity \rightarrow RF Current

$$I = \Re P_{opt}$$

Using (1) - (4) the RF output power can be now written in terms of just electrical parameters

$$P_{rf-out} = \frac{1}{2} I_{DC}^2 Z \frac{\pi V_{rf}}{V_{\pi}} \quad (5)$$

NOTE: RF power goes as the square of optical power.
RF attenuation is twice the optical attenuation (in dB).

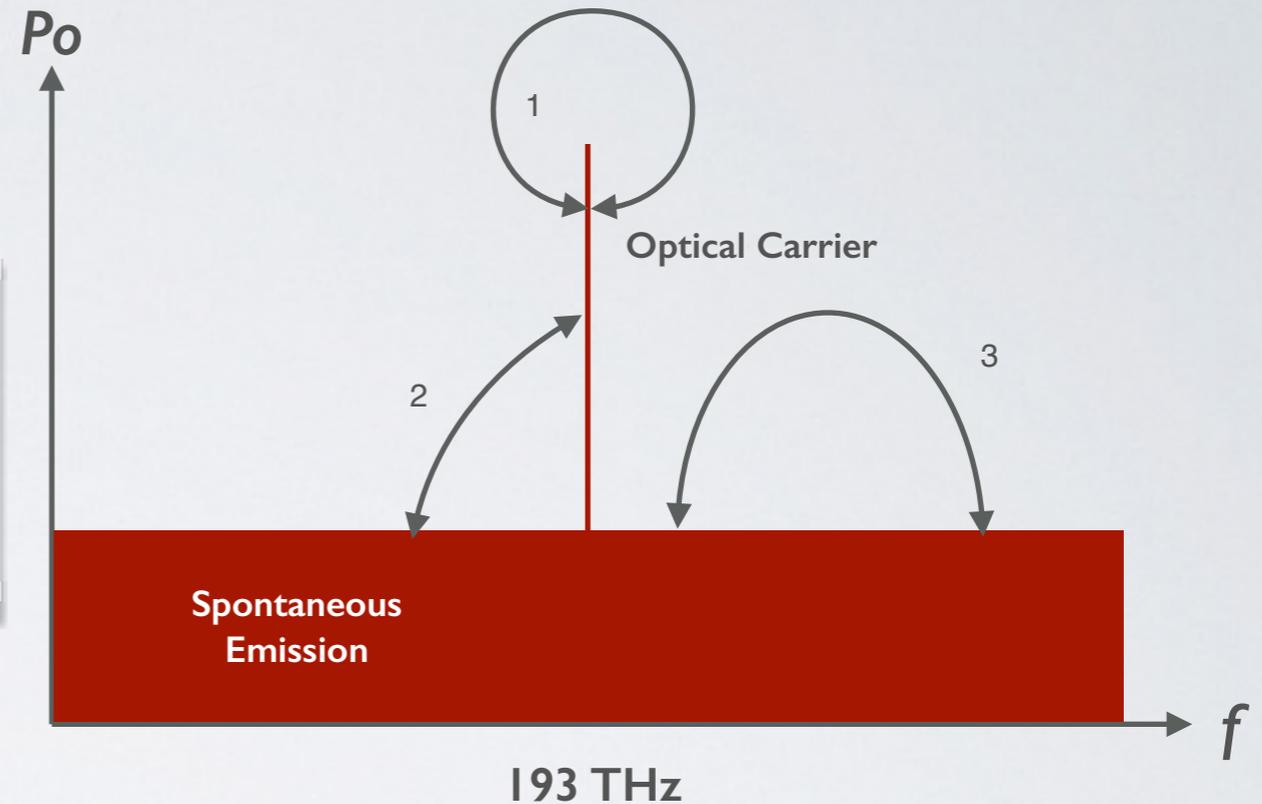
The photodiode is an optical homodyne detector

$$I \propto P_o \propto \vec{E} \cdot \vec{E}$$

[1] SIGNAL: Carrier \times Carrier = Optical Intensity

[2] NOISE: Carrier \times Spontaneous noise.

- Optical noise figure, NF_{opt}
- NF_{opt} cascades like RF noise figure.
- NF_{opt} & $G_{opt} = 0$ dB \rightarrow quantum **shot noise limit**.



$$N_{sig-sp} [dBm/Hz] = -169 + 10 \log (\Re I_{DC} [mA]) + G_{opt} [dB] + NF_{opt} [dB] \quad (6)$$

$$NF_{RF} [dB] = 174 - G_{RF} [dB] + N_{sig-sp} [dBm/Hz] \quad (7)$$

Other sources of noise are typically negligible

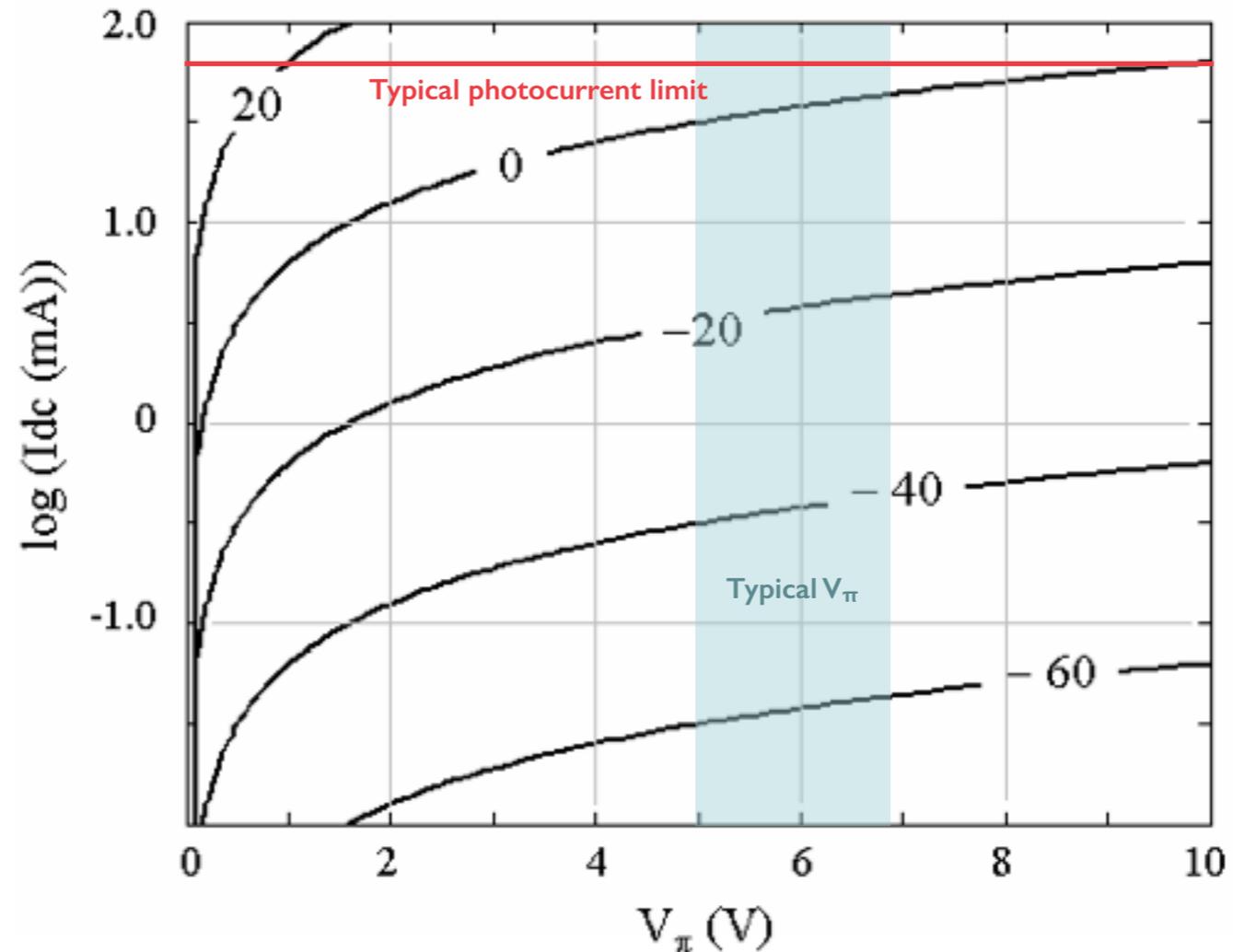
[3] - sp-sp - spont. noise heterodynes with itself.

[4] -RIN - relative intensity noise. Carrier heterodynes with its own noise sidebands (BW < 1 MHz).

Thermal Noise in the diode is negligible compared to these other products.

Calculating the RF GAIN Modulator to Photodiode

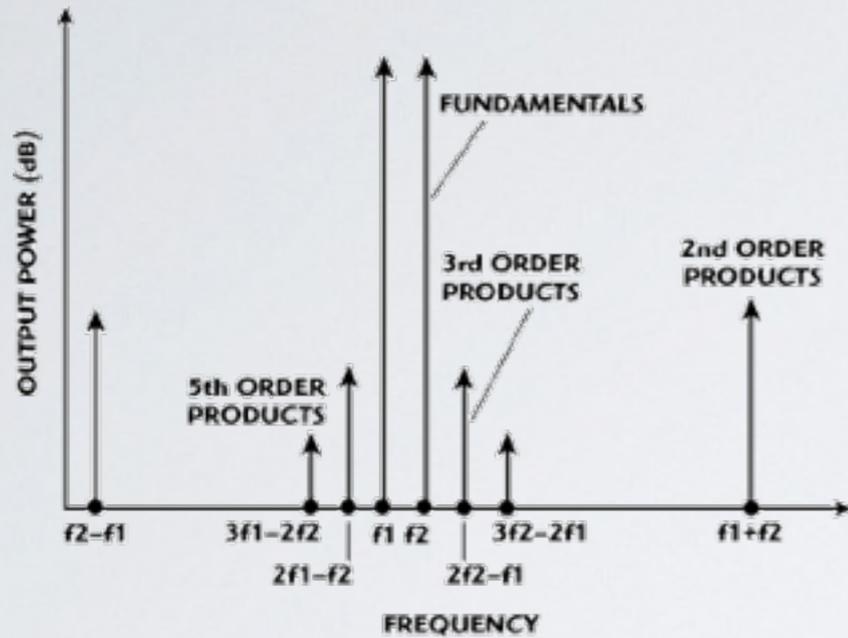
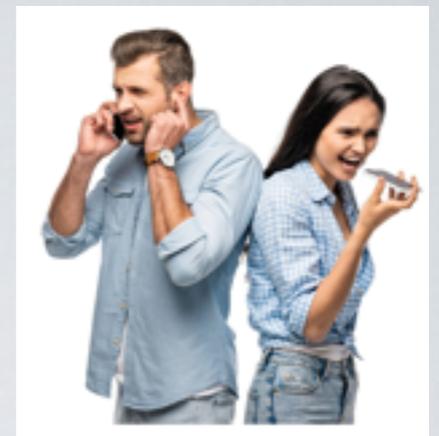
A typical link is just *slightly* lossy without added RF amplification.



$$G_{RF} = \frac{P_{rf-out}}{P_{rf-in}} = (I_{DC} Z_{\pi} / V_{\pi})^2 \quad (8)$$

$$G_{RF} [dB] = -16 - 20 \log(V_{\pi} [V]) + 20 \log(I_{DC} [mA]) \quad (9)$$

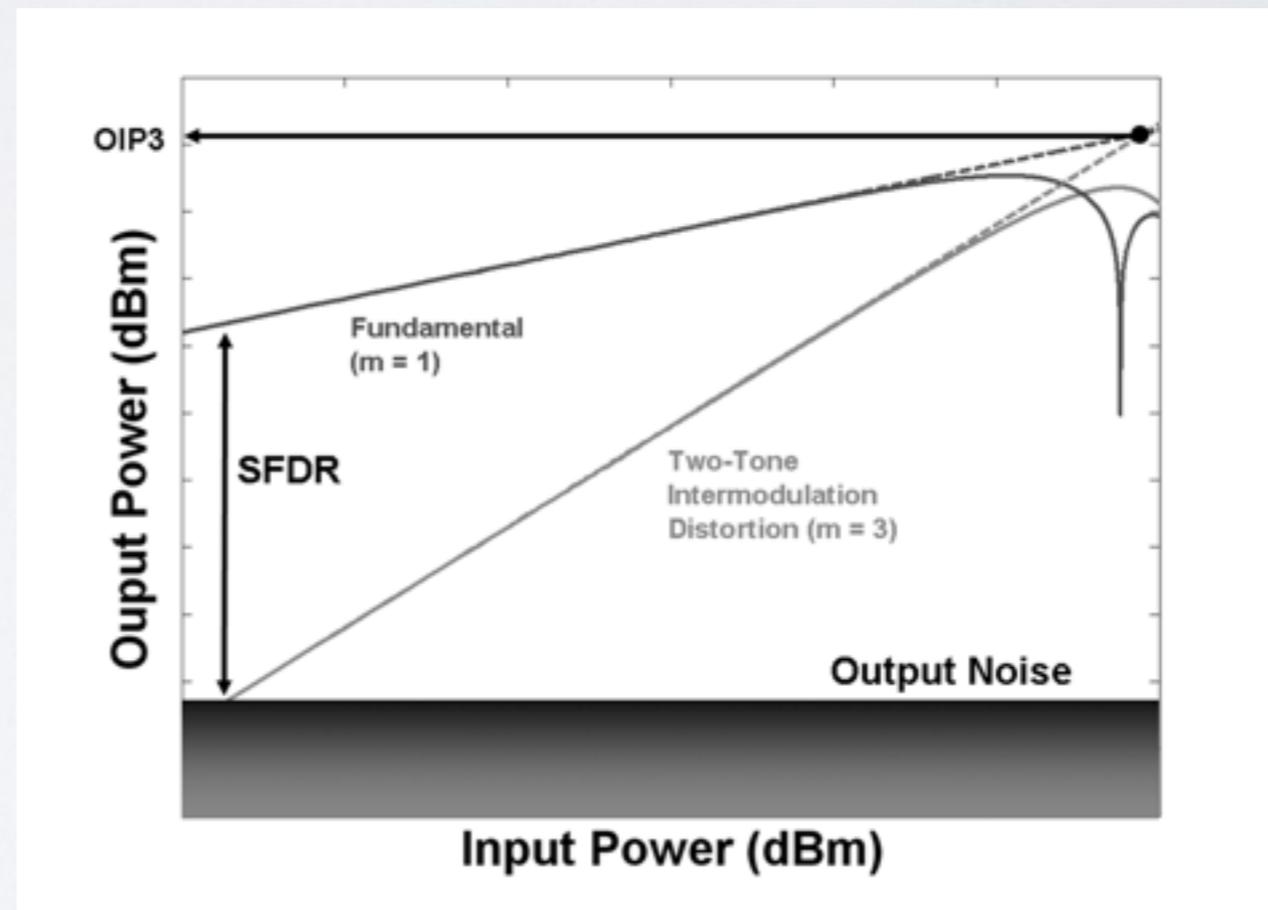
PRINCIPLE: Distortion & Dynamic Range



- 3rd-order distortion of multiple **large signals** produces adjacent spurious signals in all practical RF systems.
- +1 dB in **fundamentals** → +3 dB in 3rd order **distortion**.
- Our OIP3 can be determined from the MZM's Bessel Series.

Terminology

- *Spur-free-dynamic range* = range over which distortion is “lost in the noise.”
- *Output Third order intercept (OIP3)* is the output power where the **fundamental** and **distortion** lines intersect.



$$OIP3 [dBm] = -7 + 20 \log(I_{dc} [mA]) \quad (10)$$



We can now write down the KEY RF SYSTEM PARAMETERS

Gain

$$G_{RF} [dB] = -16 - 20 \log(V_{\pi} [V]) + 20 \log(I_{DC} [mA]) \quad (9)$$

Noise Figure

Using (7) and (9)

$$NF [dB] = 21 + 20 \log(V_{\pi} [V]) - 10 \log(\Re I_{dc} [mA]) + G_{opt} [dB] + NF_{opt} [dB] \quad (11)$$

Linearity

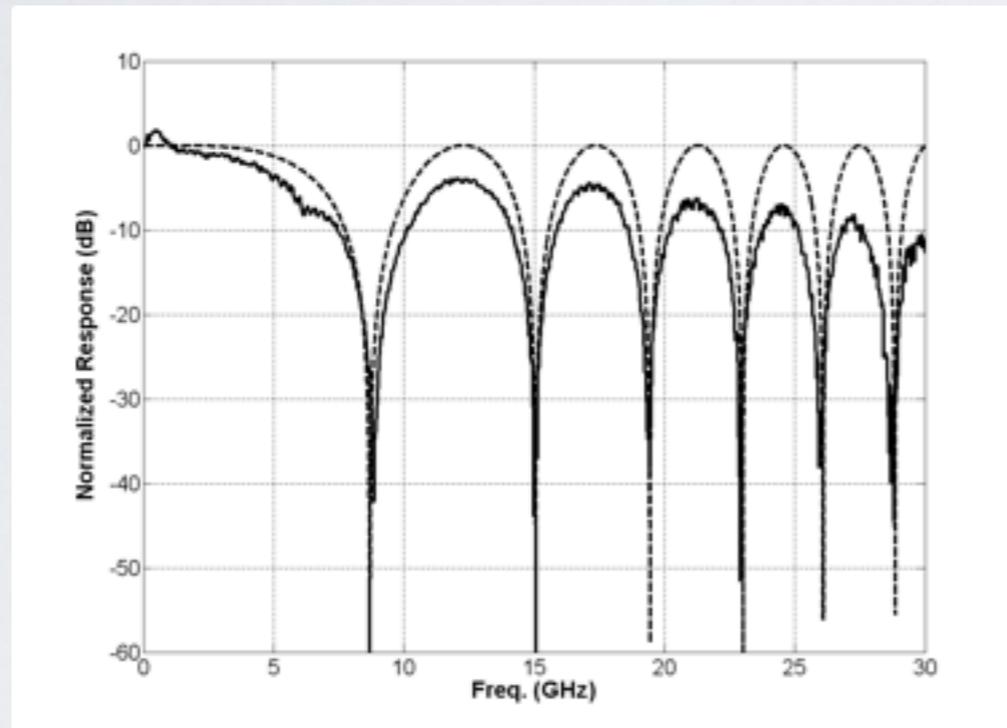
$$OIP3 [dBm] = -7 + 20 \log(I_{dc} [mA]) \quad (10)$$

TAKEAWAYS

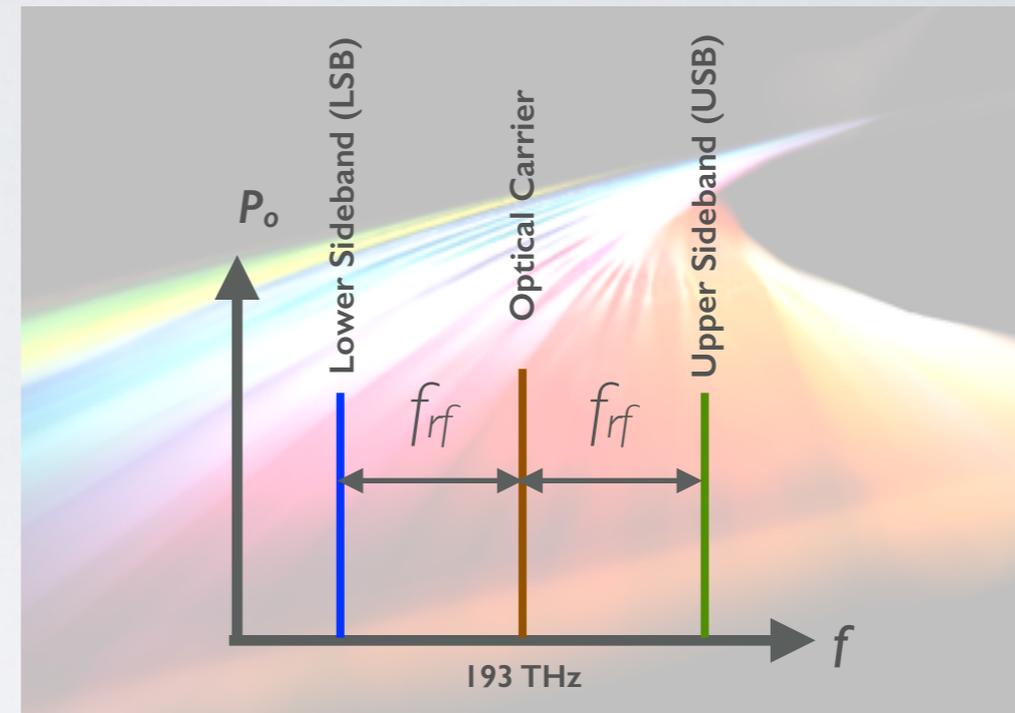
Maximize photocurrent.
Minimize the optical noise figure.
Minimize V_{π} .

Managing Dispersion

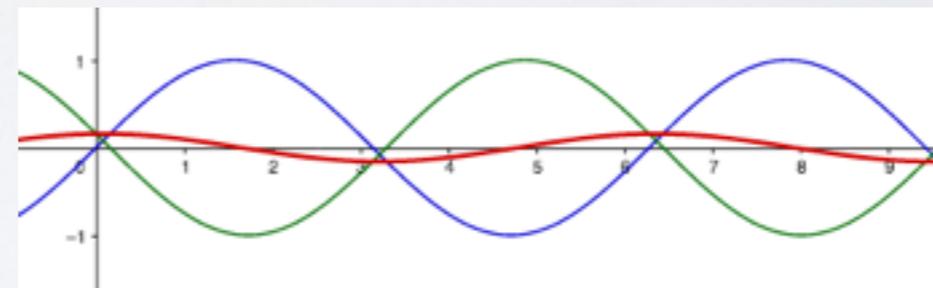
- Upper and lower sidebands travel at slightly different velocities.
- The heterodyned output from LSB and USB may get out of phase and cancel at certain frequencies.



Measured (solid) and calculated (dashed) dispersion response for a ROF channel through 50 km of SMF-28 fiber.



$$RF_{out} = (\text{carrier} \times \text{LSB}) + (\text{carrier} \times \text{USB})$$



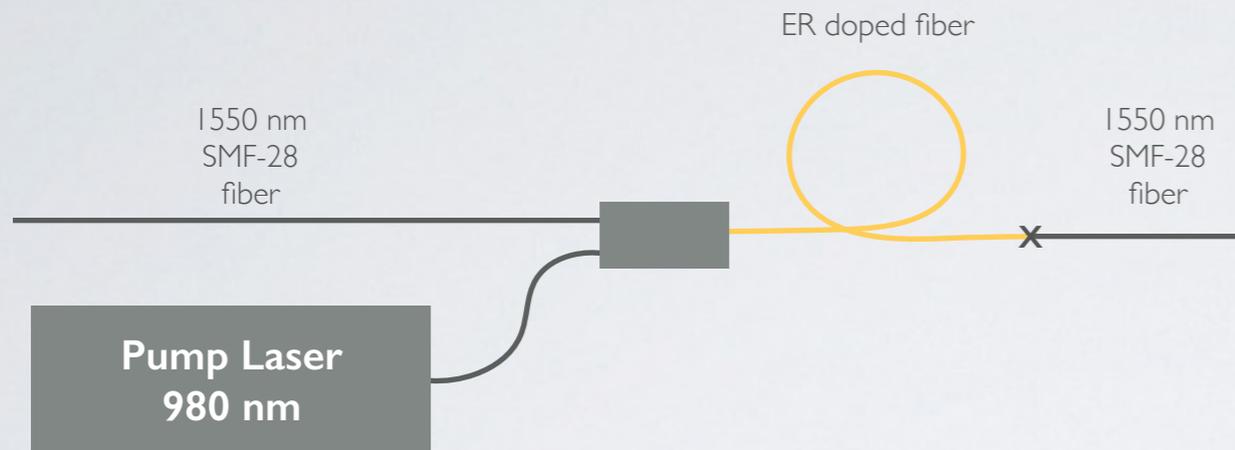
SOLUTION: Dispersion Compensating Fiber (DCF)



SMF-28®
+18 ps/nm•km

Fujikura - DCF
-155 ps/nm•km

Extending the reach to 10 km and beyond with *Erbium Doped Fiber Amplifiers*

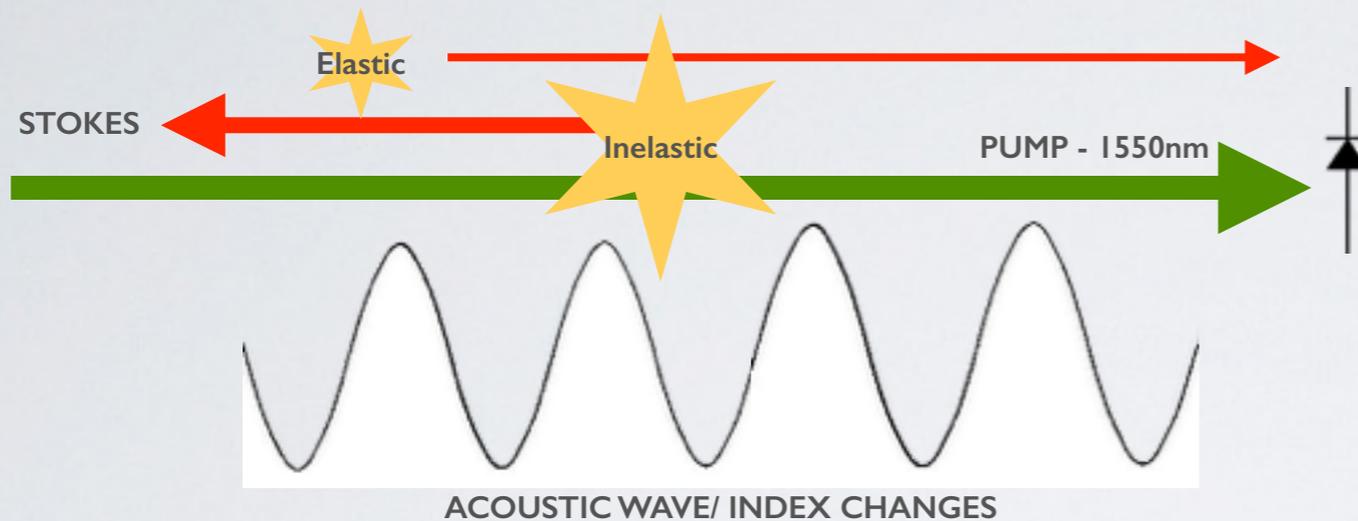


thorlabs.us
>20dB gain, 5 dB Noise Figure

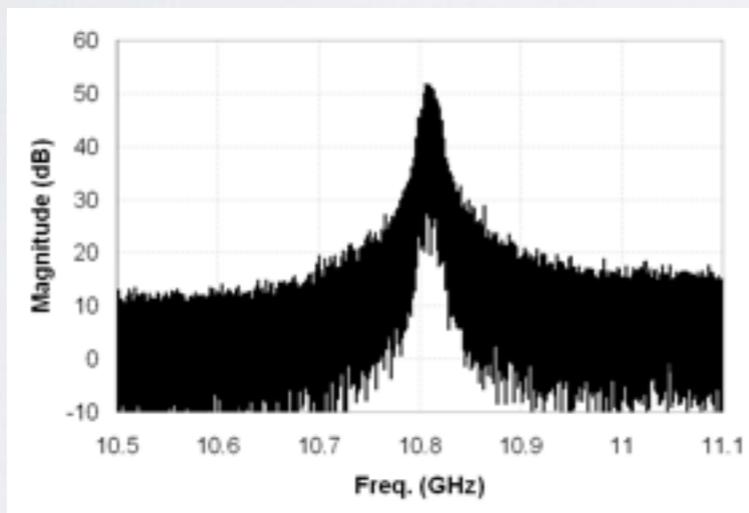
- In-fiber amplification at 1550 nm
- Inject PUMP photons at 980nm to produce an excited state in atoms
- Excited atoms produce stimulated emission at 1550nm
- 1550nm signal is amplified.
- Like a laser without end mirrors (no feedback)
- No oscillation, just amplification

Optical Power Limit

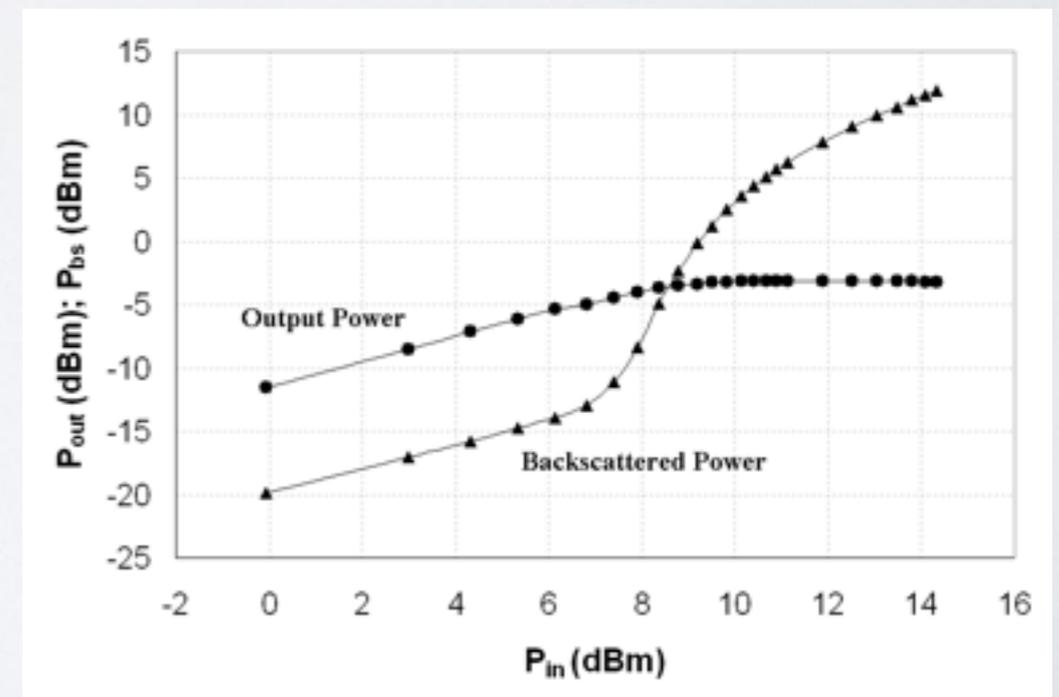
Stimulated Brillouin Scattering (SBS)



- Incident high power photons in PUMP scatter exciting vibrations in the glass.
- Acoustic waves cause ripple in refractive index (photo-elastic effect).
- Refractive index ripple forms a grating and scatters the optical signal backwards in a (red shifted) STOKES wave.
- Red shifted by resonant acoustic (phonon) frequency of ~10.8 GHz.
- Scattered forward again by (elastic) Rayleigh scattering.



Noise spectrum at the photodiode caused by Stokes wave heterodyning with Pump wave.

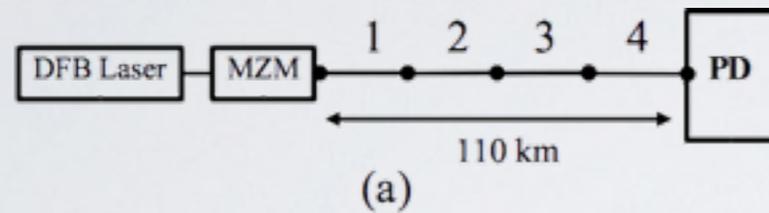


$$P_{th} \approx 21 \frac{A_{eff}}{g_B L_{eff}} \quad (12)$$

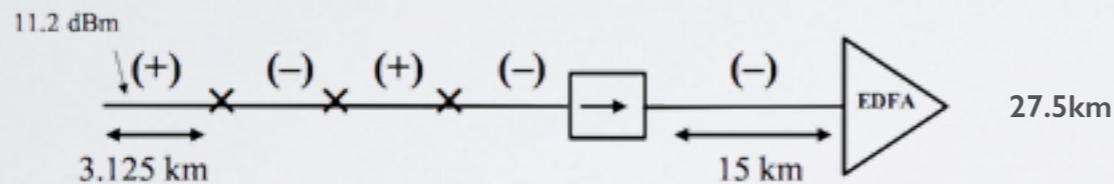
$$L_{eff} = (1 - e^{-\alpha L}) / \alpha \quad (13)$$

Long Haul Link Design

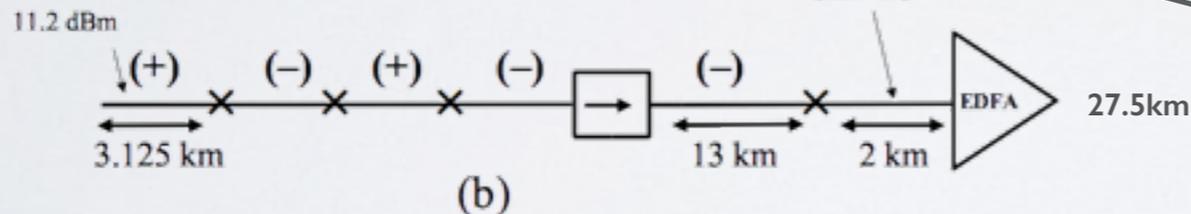
Optical Noise Figure and SBS depends on optical amplifier placement



Spans 1,2, and 3



Span 4



(+) Positive dispersion shifted fiber
 (-) Negative dispersion shifted fiber

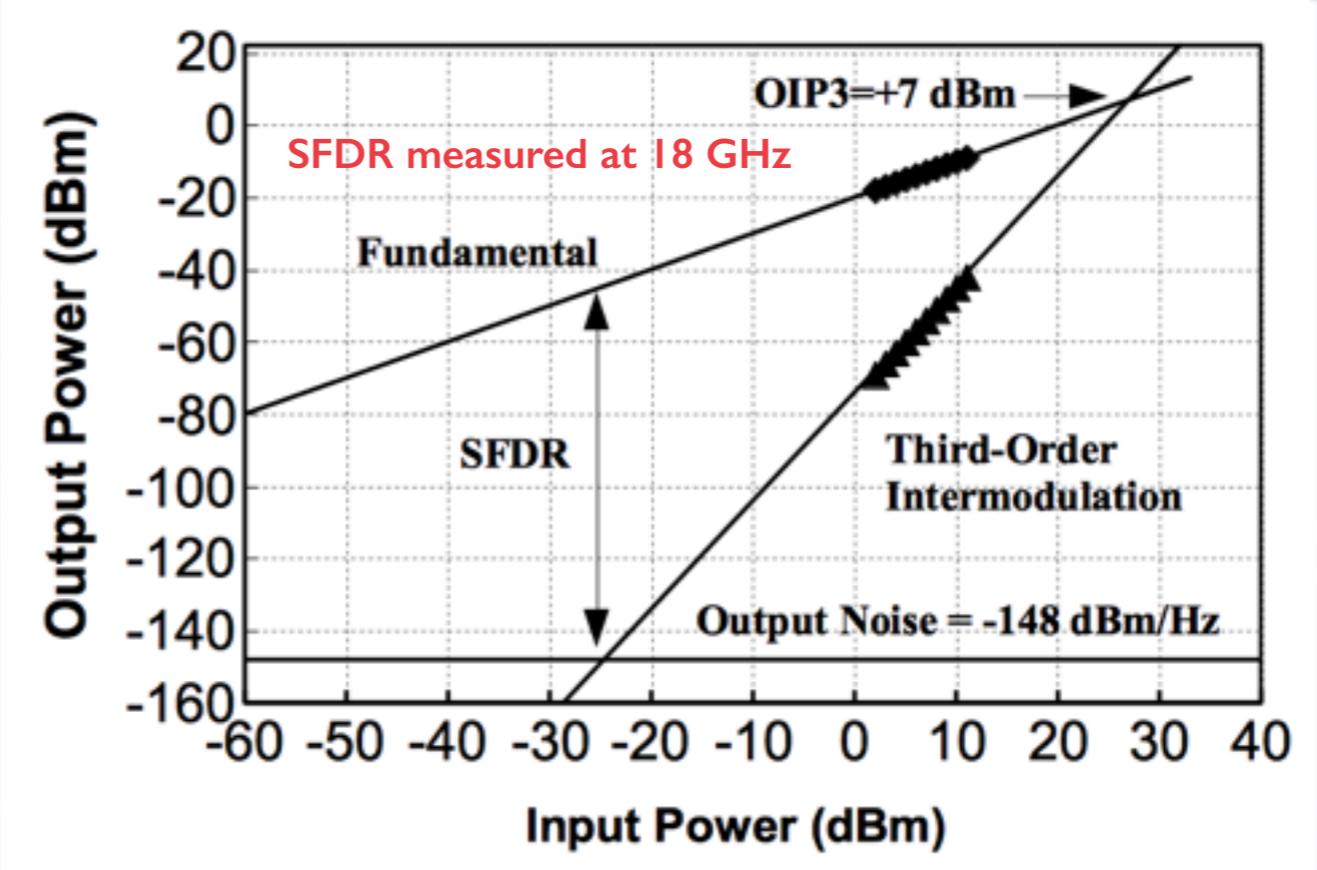
TOTAL DISPERSION = 8ps/nm
 FIRST NULL = 395 GHz
 TOTAL LENGTH = 110 km

- EDFA at launch
 - Min. NF_{opt}
 - Max. P_{opt} and SBS
- EDFA at end
 - Reduced SBS
 - Poor NF_{opt}
- Distributed amplification
 - Reasonable compromise
 - Spacing to keep P_{opt} below SBS threshold

Remember, SBS = Stimulated Brillouin Scattering

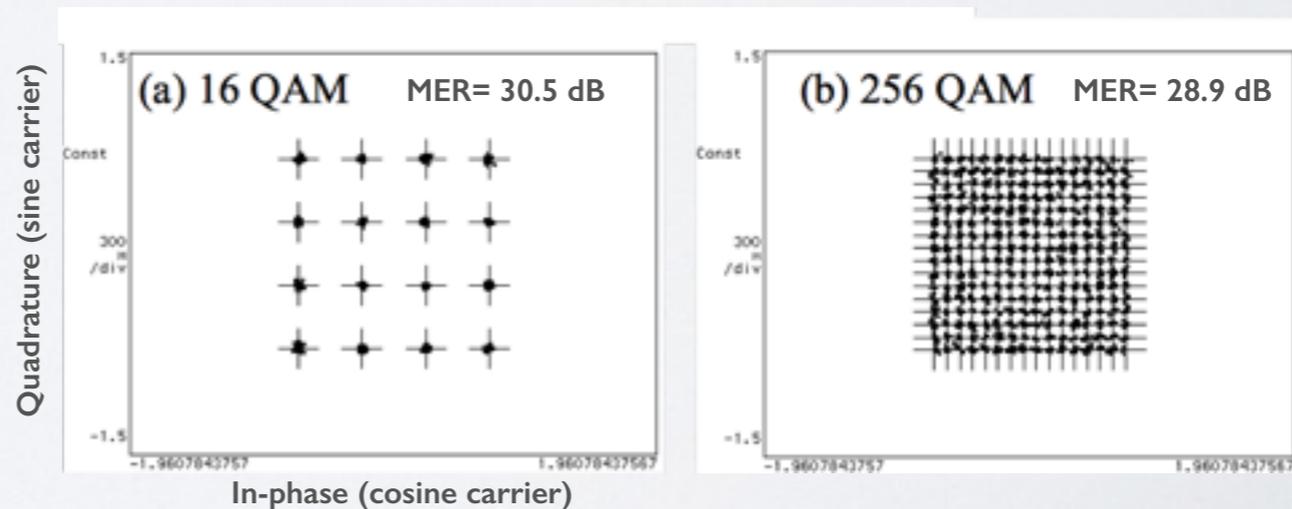
RESULTS: Excellent Dynamic Range performance over 110 km!

-  SFDR: 103 dBHz^{2/3}
- Dynamic Range is critical for multi-carrier RF applications & AM-based modulation formats
- Sufficient for 256-QAM signal with ~30dB MER



Measured Constellations

Typical of digital TV (CATV) and cable modem signal constellations.
 16-QAM encodes 4 bits/symbol & 256-QAM encodes 8 bits/symbol



5 MSymb/s @ 2 GHz



CONCLUSION

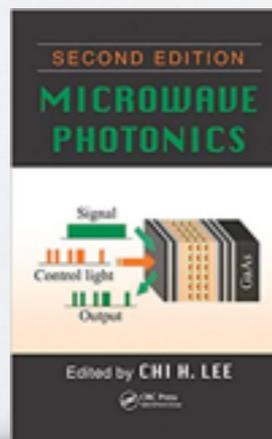
"Thank you for your time"



- Radio over Fiber can provide **low-loss** & **high dynamic range** RF links over 100 km or more!
- Simple RF link equations: Gain, Noise Figure, Dynamic Range.
- Distributed optical amplification enables long-haul links.
- Dynamic Range is limited primarily by **modulator linearity**, **Brillouin scattering**, and **optical noise** from spontaneous emission.

Learn More Here....

Download this talk: RedMountainRadio.com



Eric E. Funk, Vincent J. Urick, and Frank Bucholtz, "High Dynamic Range 100-km Digital Radio-Over-Fiber Links." in *Microwave Photonics*, Ed. Chi H. Lee, New York: CRC Press, 2006, Ch. 6.

Vincent J. Urick, Frank Bucholtz, and **Eric Funk**, "High Dynamic Range 100-km Digital Radio-Over-Fiber Links." in *Microwave Photonics*, 2nd Ed., Ed. Chi H. Lee, New York: CRC Press, 2013, Ch. 6.

